## Elements of a graph

In many experiments, we make measurements to collect data. A graph is a pictorial way of presenting a set of data. It can help analyze the data in the following ways.
1 It allows you to easily see how one physical quantity is related to another, e.g. whether they are directly proportional to each other.
2 It can be used to determine the constants in an equation relating two physical quantities, e.g. slope and intercepts of a straight-line graph.

3 It provides the best way of 'averaging' a set of data, thus reducing the effect of the errors of individual measurements.

The following example shows what elements are included in a graph.

## Example

In an experiment, a beaker of water is heated by a Bunsen burner. The temperature of the water at different time instants is measured and recorded in the table below. Plot a graph of temperature against time.

| Time $/$ min | 0 | 1 | 2 | 3 | 4 | 5 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Temperature $/{ }^{\circ} \mathbf{C}$ | 18 | 31 | 42 | 55 | 66 | 77 |

## Solution

Add the following items on graph paper.
(1) Vertical and horizontal axes
(2) Variable and unit for each axis
(3) Scale on each axis: carefully chosen to let the graph fill most of the graph paper
(4) Data points: usually marked by ' $x$ ' or ' $\odot$ '
(5) Line showing the trend: If a straightline graph is expected, draw a line of best fit. Such a straight line passes through most of the points and those not on the line are evenly spaced about it. If a straight-line graph is not expected, draw a smooth curve.
(6) Title (if necessary): describing what the graph is about

* A graph should be drawn with a sharp pencil. All straight lines (the axes and the line of best fit) should be drawn with a ruler.
(6) A graph showing the temperature of water against time during heating
temperature $1{ }^{\circ} \mathrm{C}$



## Exercise

1 What is the problem with each of the following graphs? Choose the answer from the box below.
A The axis scale is not suitably chosen.
B The axes are not properly labelled.
C The line of best fit is not correctly drawn.
D Data points are not accurately marked.
(a)

A graph of length of the liquid column in an alcohol-in-glass thermometer against temperature

(c)

A graph showing the distance travelled $s$ against time $t$

(b)

A graph showing the speed of a car against time

(d)

A graph showing the temperature $\theta$ of a metal block against time $t$


2 A hot object is allowed to cool at a constant rate. The temperature $\theta$ of the object at different time instants $t$ is recorded in the table below.

| $\boldsymbol{t} / \mathbf{m i n}$ | 0 | 10 | 20 | 30 | 40 | 50 | 60 | 70 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\boldsymbol{\theta} /{ }^{\circ} \mathbf{C}$ | 78 | 72 | 68 | 58 | 49 | 44 | 40 | 34 |

(a) (i) Plot a graph of $\theta$ against $t$ on the graph paper provided below.

(ii) Is the graph a straight line or a curve?
(b) Estimate the temperature of the object at $t=45 \mathrm{~min}$.

## Elements of a graph

3 The resistance of a thermistor in a thermistor thermometer decreases when the temperature increases.
The table below shows the resistance $R$ at various temperatures $T$.

| $\boldsymbol{T} /{ }^{\circ} \mathbf{C}$ | 0 | 8 | 16 | 24 | 32 | 40 | 48 | 56 | 64 | 72 | 80 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\boldsymbol{R} / \boldsymbol{\Omega}$ | 900 | 580 | 380 | 250 | 160 | 105 | 70 | 45 | 35 | 22 | 10 |

(a) Plot a graph to show how $R$ changes with $T$.

(b) What is the temperature when the resistance is $200 \Omega$ ?

## Answers

1 (a) $B$
(b) D
(c) C
(d) A

2 (a) (i)

(ii) A straight line
(b) At $t=45 \mathrm{~min}$, the temperature is $49^{\circ} \mathrm{C}$.

3 (a)

(b) When $R=200 \Omega$, the temperature is $28^{\circ} \mathrm{C}$.

